Beta Delayed Particle Emission

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History:

 \rightarrow 1492, the discovery of America: Shipbuilders, Caravels and the crew of Cristobal Columbus were from Huelva. Depart from a small port located at the village of Palos de la Frontera (Huelva).

→1889, first football team in Spain (soccer) founded by British workers at "Rio Tinto" mines (Rio Tinto Company, London, 1873).

→1960's, one of largest industrial sites in Spain (Chemicals, Petrol & Mining industry)

→1992, University of Huelva was born, one of the youngest Universities of Spain. (15.000 students/ 150.000 habitants of Huelva)

→1999, the Nuclear & Particle Physics group (Estructura de la Materia)





Introduction

Along history, there has been a constant effort to understand the structure and mechanism of the nature that surround us:

- Why the Universe and the Nature have the structure we observe?

- Which are the basic constituents of matter?
- How the different building blocks of matter interact which each other?
- Where, when and how the Universe has been originated?



"Creation pillars", nucleosynthesis of stars at Eagle's Nebulae



The research efforts carried out in basic nuclear physics (and Science in a wide sense) along last century (XX) has provided an un-precedent knowledge of the subatomic structure of matter and its constituents, its dynamics and the Origin of the Universe itself. From a historical point of view, the major steps in the understanding of the Universe have taken place in particle accelerators.

At present Radioctive Beam Facilities we can customize our nuclear system (N,Z), "fabricate" any nucleus controlling the number of constituent protons and neutrons.

Proton Rich Nuclei \leftarrow \rightarrow Neutron Rich Nuclei \leftarrow \rightarrow Light unbound systems \leftarrow \rightarrow Super-heavy's



→ Evolution of nuclear structure and nuclear dynamics,

 \rightarrow Exotic (N,Z) combinations \rightarrow isospin degree of freedom

- Evolution of shell structure, phase shape transitions, nucleon-nucleon pairing, spin-orbit interaction
- Halo, skin, cluster nuclear structures
- Beyond the drip lines → unbound nuclei & resonances
- Exotic decay modes and Reaction dynamics of exotic systems
- Test of astrophysical scenarios → nuclear astrophysics

Spectroscopic tools → Particle Detectors + Accelerators

Theoretical tools: Precise knowledge of theoretical framework well tested with stable nuclei → Example: DIRECT NUCLEAR REACTIONS (FRESCO, ECIS, etc,...)









Beta decay

As it was previously discussed, weak interaction is one of the vehicles used for nuclear systems to release the excess of energy and travel from drip-lines to the Valley of Stability.









Beta delayed particle emission

Emission of particles from nuclear (excited) states populated by the beta decay Two processes:

- Beta decay from the parent nucleus (precursor)
- Particle emission from excited states of "emitter" nucleus



 \rightarrow beta decay to excited levels of "emitter" nucleus; if the excited state is over separation energy Sp \rightarrow emission of particles

 \rightarrow The half-life of beta decay is much longer than the nuclear level of emitter, the half-life of the process is given by the beta decay \rightarrow "beta - delayed"

Particle emission: transitions and decaying states

The wave functions obtained by solving the Schrödinger equation for time independent potentials have the property of being stationary states

$$\hat{H}\Psi_o(r,t) = E(0)\Psi_o(r,t) \qquad \Psi_o(r,t) = \Psi_o(r)e^{-i\frac{E(0)}{\hbar}t}$$

States will remain in that energy eigenstate forever!

Under a sudden change of the potential (like beta decay $p \leftarrow \rightarrow n$), we get a new hamiltonian H_{new} and the "old" wavefunctions are no more eigenvalues \rightarrow start evolution with time:



states

protons neutrons

Some of these new

protons neutrons

are

$$\hat{U}(t)\Psi_o(r,t) = e^{-i\frac{\hat{H}_{new}t}{\hbar}}\Psi_o(r,t) = \sum c_i(t)\phi_i(r)e^{-i\frac{E(i)_{new}t}{\hbar}}$$
$$\hat{H}_{new}\phi_i(r,t) = E(i)_{new}\phi_i(r,t)$$

The transition process (particle emission) can be described by the Fermi Golden Rule

$$\lambda = \frac{2\pi}{\hbar} |V_{if}|^2 \rho(E_f)$$
$$V_{if} = \int \Psi_f^* (H_{new} - H_{old}) \Psi_i \qquad \rho(E_f) = \frac{dn_f}{dE_f}$$



- If Ef > Sp \rightarrow tunnel through Coulomb barrier \rightarrow P(r,t) decreases with time.
- → use of a complex energy eigenvalue in the final system:
 E_d + i \[\Gamma_d/2]

$$\phi_d(r,t) = N\phi_d(r)e^{-\frac{i}{\hbar}(E_d + i\Gamma_d/2)t} = N\phi_d(r)e^{-\frac{i}{\hbar}E_dt}e^{\frac{1}{\hbar}\frac{\Gamma_d}{2}t}$$

$$P(r,t) = N^2 \left|\phi_d(r,t)\right|^2 = N^2 \left|\phi_d(r)\right|^2 e^{-\frac{1}{\hbar}\Gamma_dt}$$

$$P(r,t) = N^2 \left|\phi_d(r)\right|^2 e^{-\lambda_d t} \qquad \qquad \lambda = \frac{1}{\tau} = \frac{\Gamma}{\hbar}$$

For the energy distribution (energy representation) → Fourier transform

$$\phi_d(E) \approx \int e^{-\frac{i}{\hbar}Et} \phi_d(t) dt \approx \int e^{-\frac{i}{\hbar}Et} e^{-\frac{i}{\hbar}E_d t} e^{-\frac{1}{\hbar}\frac{\Gamma}{2}t} dt$$
$$\phi_d(E) \approx \frac{1}{(E - E_d) + i\frac{\Gamma}{2}} \qquad P(E) \approx \frac{1}{(E - E_{dec})^2 + \left(\frac{\Gamma}{2}\right)^2}$$



Why complex eigenvalues? $\rightarrow E_d + i \Gamma_d/2 \rightarrow$ naturally arise from solving Shrödinger ecuation at E>0! <u>Georg Gamow</u>: simple model of alpha decay, G.A. Gamow, Zs f. Phys. 51 (1928) 204; 52 (1928) 510 \rightarrow Quantum tuneling through barrier V $u''(r) = \left[\frac{l(l+1)}{r^2} + \frac{2\mu}{\hbar^2}V(r) - k^2\right]u(r)$ REDHI GIVE COULOMB BARRIER $u(r)\sim C_0 \; r^{l+1}$, r
ightarrow 0E_{kin} $u(r) \sim C_+ H^+_{l,n}(kr)$, $r \to +\infty$ (bound, resonant) $u(r) \sim C_+ H^+_{l,n}(kr) + C_- H^-_{l,n}(kr)$, $r \to +\infty$ (scattering) n ATTRACTIVE NUCLEAR POTENTIAL If keep same boundary condition \rightarrow H⁺(kr), r $\rightarrow \infty$ Bound and resonant states \rightarrow poles of the 0.8 Scattering matrix S(k) (matching with outgoing WF) 0.4 Bound states: → pure imaginary K values: ~ - i Ki, Er < 0</p> Resonant states: → complex K values: Kr - i Ki, Er > 0, F> 0 0.8 → GAMOW STATES 40 80 r [fm] Figure 1: Gamow radial wave function $\varphi_{nl}(r)$ $\hat{1} = \sum_{i=h} |u_i
angle \langle ilde{u}_i| + \sum_{i=r} |u_j
angle \langle ilde{u}_j| + \int_{L^+} |arphi(k)
angle dk \langle ilde{arphi}(k^*)|$

Consistent description of bound and scattering states: \rightarrow a rigged Hilbert space (Gel'fand triple space): 1960s Gel'fand combined Hilbert space with the theory of distributions.

Spectacular applications: Shell model in the continuum// → Shell model in the complex energy plane; N. Michel, W. Nazarewicz, M. Oloszajzak and T. Vertse (J. Phys. G.: Nucl. Part. Phys. 36 (2009) 013101

Difficult to overstimate the importance of Gamow theory!!.

Some references: Humblet and Rosenfeld, Nucl. Phys. 26, 529 (1961); T. Berggren, Nucl. Phys. A 109 (1968) 265. R. de la Madrid, Nucl. Phys. A812, 13 (2008)

R-MATRIX DESCRIPTION

Tradicional method → based on R-matrix theory for unbound nuclei → scattering, reactions, particle decay. (F. C. Barker, Aust. J. Phys., 1988, 41, 743-63, E.K. Warburton, PRC 33 (1986)303-313)



Gamow states of a finite potential



SUMMARY: what to expect for beta delayed particle emission

Two processes:

- Beta decay \rightarrow FERMI INTEGRAL (Matrix elements) \rightarrow (Q-En)⁵
- Particle emission → BARRIER PENETRABILITY ~ P(Ek) ~ 1/(1+ exp((EB-Ek)/wb) (parabolic)
- Breit Wigner shapes on each level
- Density of states above Sp



history \rightarrow observed since early stages of nuclear physics:

Beta delayed alphas ($\beta\alpha$): Rutherford (1916) [*Philos. Mag.* **31** (1916) 379] \rightarrow "Long range alpha particles followed by beta decay of 212Bi"

Beta delayed protons (βp): Marsden (1914) \rightarrow ¹⁴N(α ,p)¹⁷O [*Philos. Mag.* **37** (1919) 537]; Álvarez (1950) bombarded ¹⁰B and ²⁰Ne with 32 MeV protons \rightarrow beta delayed ⁸B, ²⁰Na α -emitters

The modern era begins in 1960's (βp, β2p)/ Zeldovich, Karnaukhov, Goldansky... [Goldanskii NPA 19 (1960) 482]

 Spectroscopic tool: Information about level energies, spins and parities of participant nuclei (precursor, emitter, daughter)

At present days investigations on beta delayed radioactivity are very intense, particularly with the use of radioactive beams:

typical decay mechanism at drip lines

- Large Qb values \rightarrow access high energy states Good alternative to gamma spectroscopy and nuclear reactions limited by beam intensities ~10⁴ pps

- Beta delayed particle emission \rightarrow limited by selection rules of beta decay

- Usually first type of studies close to drip lines \rightarrow low isotope production \rightarrow largest yields obtained directly after ion source and implanted on decay foil.

- Relatively "simple" experimental setups.



TYPICAL EXPERIMENTAL SETUP



Beta delayed particle emitters



Example: The case of beta delayed particle emission from 31Ar (Z=18, N=13)









Fig. 4. The proposed level scheme and decay mechanism for ³¹Cl. Energy levels are given in MeV, relative to the ground state of ³¹Cl. (*) means ambiguous assignment; see text for details.

SUMMARY

We have revised the physics concepts behind the beta delayed particle emission process:

- Basic ides about the exotic decay process

- Exotic decays are an important source of spectroscopic information: level energies, spins, B(F) and B(GT) values, etc

- Technical aspects to measure these decay modes
- Status of beta delayed nucleon emission
- Basic ideas for beta decay and isospin
- Simple models for particle emission (Gamow states, R-Matrix,...)

THANKS FOR YOUR ATTENTION ...